



Optimal algorithm for phase shift searching for the DPSBF

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- Spatial signal filtering
- Any technique which can change the radiation pattern

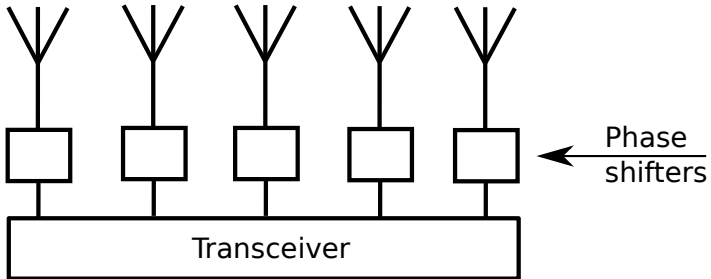
Phase shift beamforming



Antenna array

Centralized phase shift beamforming

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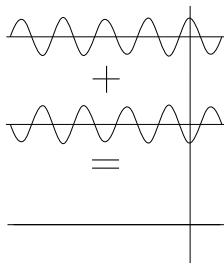
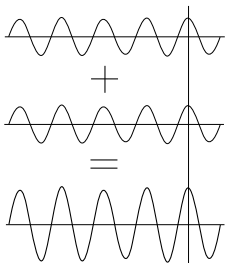




Phase shift beamforming

The principle

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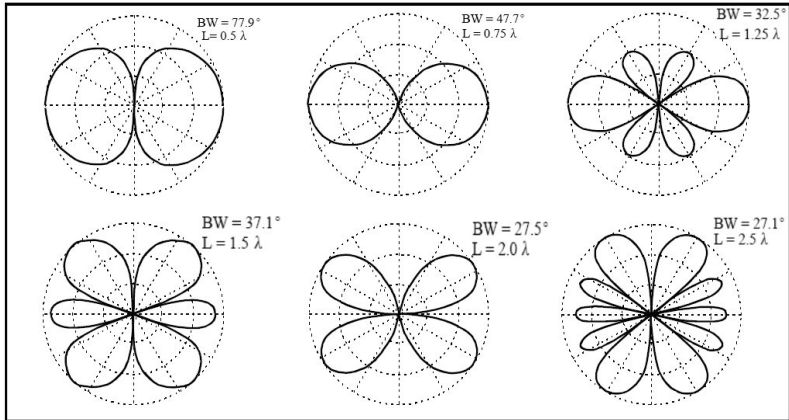




Phase shift beamforming

Examples

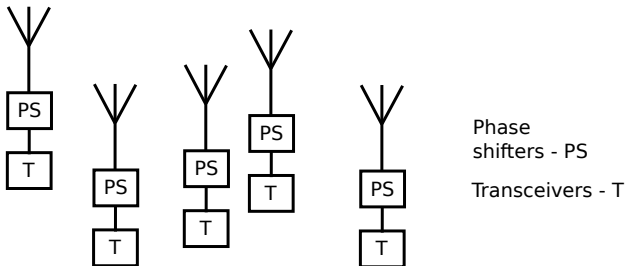
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Distributed phase shift beamforming

The principle of the antenna array without central transmitter and with unknown antenna positions.

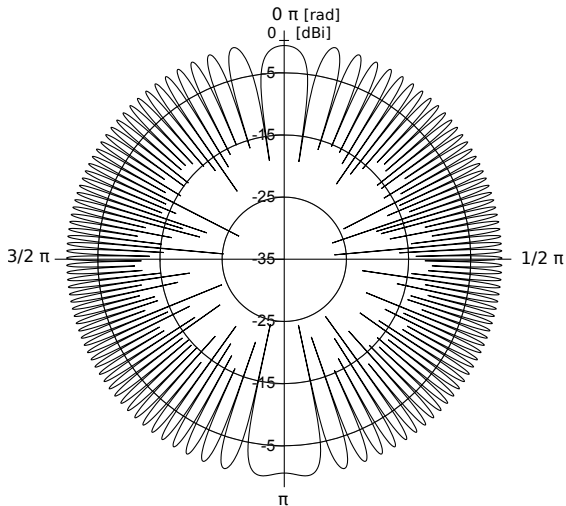




DPSBF - radiation pattern

Phase shift $\pi/3$, two transmitters, 30 wavelengths distance

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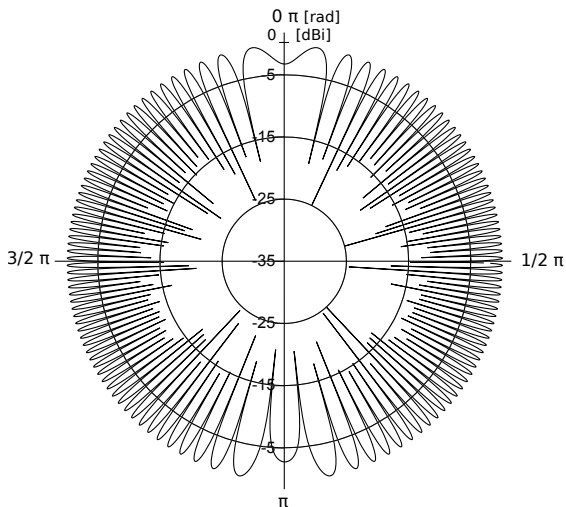




DPSBF - radiation pattern

Phase shift $\pi + \pi/3$, two transmitters, 30 wavelengths distance

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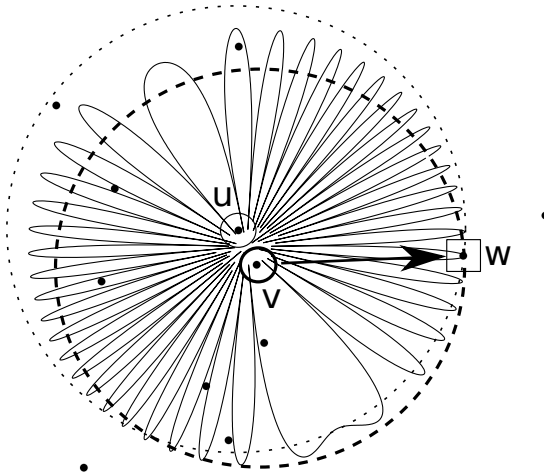




Interference cancellation

Basic principle

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Problem definition

Phase shift searching across the network

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$$trNumber = 2 * |E| * (avgNeigh - 1) * (360/MS + 2) \quad (1)$$

$$n = 360/MS \quad (2)$$

$$complexity = O(n) \quad (3)$$



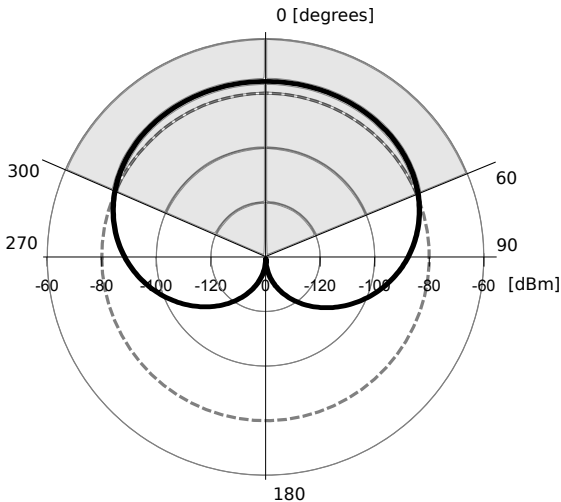
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Phase shift searching

What is it about?

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Phase shift searching

Stage 1

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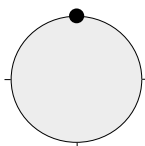
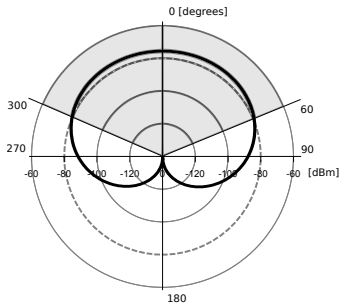
```
1:  $SS \leftarrow 360$                                 ▷ Current searching step size
2:  $used \leftarrow$  empty set                        ▷ Set of all checked values for  $SS$ 
3: while  $SS > MS$  do                               ▷  $MS$  is the minimal step
4:    $p \leftarrow 0$ 
5:   for  $p < (360/SS)$  do
6:     if  $s \notin used$  then
7:       send( $s$ , destination);  $used \leftarrow s$ 
8:     end if
9:      $p \leftarrow p + 1$ 
10:  end for
11:   $SS \leftarrow SS/2$ ; ask the destination host for the results
12:  if destination received signal then
13:     $phase \leftarrow$  best received phase; break
14:  end if
15: end while
```



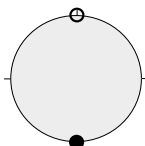
Phase shift searching

Stage 1 - progress example

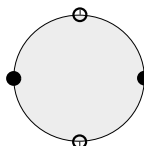
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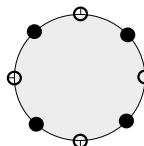
SS=360



SS=180



SS=90



SS=45



- 1: $phase \leftarrow$ best confirmed phase from the Stage 1
- 2: SS remains unchanged from the Stage 1
- 3: **while** $SS > MS$ **do**
- 4: send($phase + SS$, destination)
- 5: send($phase - SS$, destination)
- 6: ask the destination for the result
- 7: according the confirmation do:
- 8: $phase \leftarrow [phase + SS | phase - SS | SS]$
- 9: $SS \leftarrow SS/2$
- 10: **end while**



Phase shift searching

Algorithm

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```
1:  $phase \leftarrow 0$ 
2: execute the Stage 1
3: if the Stage 1 was successful then
4:     execute the Stage 2
5:     return  $phase$ 
6: else
7:      $\triangleright$  The Stage 1 did not find the usable phase shift
8:     return ERROR
9: end if
```



Maximal number of transmissions

$$3 + \sum_{i=0}^{\log_2(n)} (2^i + 2) \quad (4)$$

Best case complexity

$$\Omega(1) \quad (5)$$

Worst case complexity

$$O(n + \log_2(n)) \quad (6)$$





Number of transmissions

$$4 \log_2(n) \quad (7)$$

Complexity

$$\Theta(\log_2(n)) \quad (8)$$



Best case complexity

$$\Omega(\log_2(n)) \quad (9)$$

Worst case complexity

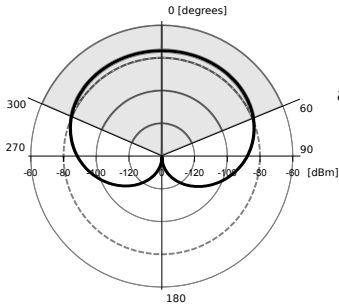
$$O(n + \log_2(n)) \quad (10)$$



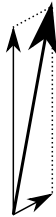
Stage 1 of the proposed algorithm finishes the most in two steps in all possible cases.



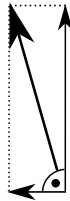
Proof of theorem



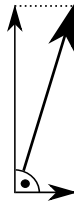
a)



b)



c)





$$\Theta(\log_2(n)) \quad (11)$$



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Improvement

The complexity of the phase searching was improved from the linear complexity to the logarithmic.



Thank you for your attention!